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| **Ilsington C of E Primary**  **Mathematics Curriculum Plan Years 1-6** |

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| Intent |
| Our aim at Ilsington is to equip all pupils with the skills and confidence to develop a deep and conceptual understanding of maths in preparation for life beyond school. Children are encouraged to develop curiosity about number and embrace the mathematics that surrounds them each day in a variety of contexts. Maths at Ilsington is an opportunity to take risks, be challenged and to work both independently and collaboratively.  The intent of our mathematics curriculum is to teach a rich, engaging and balanced curriculum which builds on previously acquired knowledge and skills. Children will become fluent in the fundamentals of mathematics then develop their skills to be able to reason and problem solve. They will develop resilience and self-confidence when faced with mathematical challenges and have the chance to believe in themselves as mathematicians. They will embrace their mistakes as part of the learning process and value the importance of effort. They will recognise that mathematics underpins much of our daily lives and make connections between what is learnt in the classroom and the wider world as well as applying their mathematical knowledge to other subjects. |

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| **Implementation** |
| We ensure our children have access to a high quality maths curriculum that is both challenging and enjoyable.  Objects, pictures, words, numbers and symbols are displayed in each class. The mastery approach incorporates all of these to help children explore and demonstrate mathematical ideas, enrich their learning experience and deepen understanding. Together, these elements help cement knowledge so pupils truly understand what they’ve learnt. All pupils, when introduced to a key new concept, will have the opportunity to build competency in this topic by taking this approach. Pupils are encouraged to physically represent mathematical concepts. Objects and pictures are used to demonstrate and visualise abstract ideas, alongside numbers and symbols.    **Concrete** – children have the opportunity to use concrete objects and manipulatives to help them understand and explain what they are doing.  **Pictorial** – children then build on this concrete approach by using pictorial representations, which can then be used to reason and solve problems.  **Abstract** – With the foundations firmly laid, children can move to an abstract approach using numbers and key concepts with confidence.    Planning  Our planning ensures we fully develop independent learners with inquisitive minds who have secure mathematical foundations and an interest in wanting to get better and do the challenges set.  At Ilsington, our short term planning is based on the Maths No Problem materials to support teaching and learning in Y1-Y6 alongside our calculation policy, NCETM and NRICH materials. Similarly, EYFS use the White Rose materials to plan the teaching inputs and continuous provision, and supplement this with resources from Hamilton Trust and NRICH.  A detailed, structured curriculum is mapped out across all phases ensuring continuity and a calculation policy is used to ensure a consistent approach. Each unit of mathematics is taught in a sequence which has been planned based on formative assessment of what the children already know. Elicitation tasks are carefully designed by the teachers at the start of every unit to inform the planning cycle. New content is taught through small steps to support children in their learning journey which progresses into supported and independent practise for children to secure their new skills. Teachers use differentiated questioning to elicit feedback from all students to expose and address any misconceptions in learning. Where these misconceptions are seen, they are readdressed through supported practice to enable all children to succeed. Concrete and pictorial representations of mathematics are carefully chosen to help build procedural and conceptual knowledge. Additional models, visuals and manipulatives are used to scaffold children who may struggle to grasp concepts and challenges are provided for those who grasp them quickly. These focus on breadth and depth of understanding and the children are expected to apply their knowledge in challenging scenarios.  Lesson Structure and Classroom Management  In Reception and Year 1 the day starts with a practical task, usually outside, to explore and recap mathematical concepts. From Year 2, the school day typically begins with a fluency task which provides a daily opportunity to recap core mathematical understanding and address misconceptions of all areas of the maths curriculum.  Depending on class structure, as mixed-age classes dictate, year groups may receive separate lesson inputs by the class teacher and sometimes will share the direct teaching, but all will have differentiation incorporated into each lesson.  Throughout the lesson, teachers will challenge understanding through regular, investigative questioning, for example: How do you know? Can you prove it? Are you sure? What’s the same/different? Can you explain that? Can you find another way of doing that? Maths pairs and trios are used as well as whole class discussions as forums for expanding thinking and sharing reasoning to deepen understanding. Responses are expected using the correct mathematical vocabulary and sentence stems are used to support and encourage this.  The main body of the lesson will include concrete, pictorial and abstract forms of mathematical learning and opportunities to develop fluency, problem-solving and reasoning. Lessons conclude with a review question which is a five-minute discussion to reflect upon the learning of the lesson and will form the recap question at the start of the next lesson.  Vocabulary and Displays  Rich maths vocabulary is frequently modelled and discussed by class teachers and pupils. The expectations are high for children to consistently use accurate, concise and age-appropriate mathematical vocabulary during discussions and in written reasoning. Teachers regularly address misconceptions and dual-meanings so that by the children reach the end of Year 6, they have a clear understanding of KS1 and KS2 maths language to eliminate potential barriers to understanding SATs questions. Moreover, they are able to use this language correctly in real life contexts outside of school.  The vocabulary for the current topic is displayed on the maths wall in the classroom, alongside children’s work and relevant imagery, numbers and symbols, for children to refer to and to support their learning.  Children know where their maths resources are and are encouraged to independently use them to assist their own learning.  SEND and Mop-up Maths  Some individuals are specifically supported by additional adults, resources or differentiated activities in Maths. Learners who need further support have an opportunity for “Mop-up Maths” sessions later in the day or following morning. Interventions for pupils working significantly below age-related expectation will be detailed in class provision maps.  AFL, editing and feedback  Assessment in maths is formative and summative with the sole purpose of moving children’s learning forwards. Children are fully involved in the process through peer and self-assessment as well as discussions with the class and the teacher. They are given opportunities to check their work and correct mistakes. Children are given time to respond to feedback using a purple pen or verbally as part of a discussion.  Times Tables  From Year 2, regular, short times tables activities take place in each class either during or before a maths lesson. All children from Year 1 upwards have access to Times Tables Rockstars (TTRS), a web-based multiplication program which children can access both at home and at school; Year 4 pupils use this facility to practise for the Multiplication Tables Check. All KS1 and KS2 children learn number facts or their times tables as part of home learning. As a result, our children develop confident recall of multiplication tables up to 12x12 by the end of Year 4. |

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| Impact |
| Children at Ilsington will develop confidence, understanding and enjoyment in mathematics along with a comprehensive set of problem-solving skills and strategies to take with them to the next stage of their education and to make use of throughout life. They will be engaged, resilient and challenged and able to quickly recall facts and techniques. They will use mathematics effectively as a tool in a wide variety of situations and will be able to present a justification or argument relating to a problem using mathematical language. They will understand the relevance of what they are learning in relation to real world concepts and develop a sense of curiosity about the subject. |

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| **National Curriculum aims:** |
| **The National Curriculum for Mathematics aims to ensure that all pupils:**   * become fluent in the fundamentals of mathematics, including through varied and frequent practice with increasingly complex problems over time, so that pupils develop conceptual understanding and the ability to recall and apply knowledge rapidly and accurately. * reason mathematically by following a line of enquiry, conjecturing relationships and generalisations, and developing an argument, justification or proof using mathematical language * can solve problems by applying their mathematics to a variety of routine and non-routine problems with increasing sophistication, including breaking down problems into a series of simpler steps and persevering in seeking solutions. |

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| **Our Progressive Curriculum Plan** | | | | | |
| **Number and place value** | | | | | |
| **Counting** | | | | | |
| **Year 1** | **Year 2** | **Year 3** | **Year 4** | **Year 5** | **Year 6** |
| count to and across 100, forwards and backwards, beginning with 0 or 1, or from any given number |  |  | count backwards through zero to include negative numbers | interpret negative numbers in context, count forwards and backwards with positive and negative whole numbers, including through zero | use negative numbers in context, and calculate intervals across zero |
| count, read and write numbers to 100 in numerals; count in multiples of twos, fives and tens | count in steps of 2, 3, and 5 from 0, and in tens from any number, forward or backward | count from 0 in multiples of 4, 8, 50 and 100; | count in multiples of 6, 7, 9, 25 and 1 000 | count forwards or backwards in steps of powers of 10 for any given number up to 1 000 000 |  |
| given a number, identify one more and one less |  | find 10 or 100 more or less than a given number | find 1 000 more or less than a given number |  |  |
| **Comparing numbers** | | | | | |
| use the language of: equal to, more than, less than (fewer), most, least | compare and order numbers from 0 up to 100; use <, > and = signs | compare and order numbers up to 1 000 | order and compare numbers beyond 1 000 | read, write, order and compare numbers to at least 1 000 000 and determine the value of each digit *(appears also in Reading and Writing Numbers)* | read, write, order and compare numbers up to 10 000 000 and determine the value of each digit (appears also in Reading and Writing Numbers) |
| *compare numbers with the same number of decimal places up to two decimal places* *(copied from Fractions)* |
| **Identifying, representing and estimating numbers** | | | | | |
| identify and represent numbers using objects and pictorial representations including the number line | identify, represent and estimate numbers using different representations, including the number line | identify, represent and estimate numbers using different representations | identify, represent and estimate numbers using different representations |  |  |
| **Reading and writing numbers (including Roman numerals)** | | | | | |
| read and write numbers from 1 to 20 in numerals and words. | read and write numbers to at least 100 in numerals and in words | read and write numbers up to 1 000 in numerals and in words |  | read, write, order and compare numbers to at least 1 000 000 and determine the value of each digit *(appears also in Comparing Numbers)* | read, write, order and compare numbers up to 10 000 000 and determine the value of each digit *(appears also in Understanding Place Value)* |
| *tell and write the time from an analogue clock, including using Roman numerals from I to XII, and 12-hour and 24-hour clocks*  *(copied from Measurement)* | read Roman numerals to 100 (I to C) and know that over time, the numeral system changed to include the concept of zero and place value. | read Roman numerals to 1 000 (M) and recognise years written in Roman numerals. |
| **Understanding place value** | | | | | |
|  | recognise the place value of each digit in a two-digit number (tens, ones) | recognise the place value of each digit in a three-digit number (hundreds, tens, ones) | recognise the place value of each digit in a four-digit number (thousands, hundreds, tens, and ones) | read, write, order and compare numbers to at least 1 000 000 and determine the value of each digit *(appears also in Reading and Writing Numbers)*  *recognise and use thousandths and relate them to tenths, hundredths and decimal equivalents (copied from Fractions)* | read, write, order and compare numbers up to 10 000 000 and determine the value of each digit *(appears also in Reading and Writing Numbers)* |
| *find the effect of dividing a one- or two-digit number by 10 and 100, identifying the value of the digits in the answer as units, tenths and hundredths (copied from Fractions)* | *identify the value of each digit to three decimal places and multiply and divide numbers by 10, 100 and 1 000 where the answers are up to three decimal places (copied from Fractions)* |
| **Rounding** | | | | | |
|  |  |  | round any number to the nearest 10, 100 or 1 000 | round any number up to 1 000 000 to the nearest 10, 100, 1 000, 10 000 and 100 000 | round any whole number to a required degree of accuracy |
|  |  |  | *round decimals with one decimal place to the nearest whole number (copied from Fractions)* | *round decimals with two decimal places to the nearest whole number and to one decimal place (copied from Fractions)* | *solve problems which require answers to be rounded to specified degrees of accuracy (copied from Fractions)* |
| **Problem solving** | | | | | |
|  | use place value and number facts to solve problems | solve number problems and practical problems involving these ideas. | solve number and practical problems that involve all of the above and with increasingly large positive numbers | solve number problems and practical problems that involve all of the above | solve number and practical problems that involve all of the above |

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| **Addition and subtraction** | | | | | |
| **Number bonds** | | | | | |
| **Year 1** | **Year 2** | **Year 3** | **Year 4** | **Year 5** | **Year 6** |
| represent and use number bonds and related subtraction facts within 20 | recall and use addition and subtraction facts to 20 fluently, and derive and use related facts up to 100 |  |  |  |  |
| **Mental calculation** | | | | | |
| add and subtract one-digit and two-digit numbers to 20, including zero | add and subtract numbers using concrete objects, pictorial representations, and mentally, including:   * a two-digit number and ones * a two-digit number and tens * two two-digit numbers * adding three one-digit numbers | add and subtract numbers mentally, including:   * a three-digit number and ones * a three-digit number and tens * a three-digit number and hundreds |  | add and subtract numbers mentally with increasingly large numbers | perform mental calculations, including with mixed operations and large numbers |
| read, write and interpret mathematical statements involving addition (+), subtraction (-) and equals (=) signs *(appears also in Written Methods)* | show that addition of two numbers can be done in any order (commutative) and subtraction of one number from another cannot |  |  |  | use their knowledge of the order of operations to carry out calculations involving the four operations |
| **Written methods** | | | | | |
| read, write and interpret mathematical statements involving addition (+), subtraction (-) and equals (=) signs *(appears also in Mental Calculation)* |  | add and subtract numbers with up to three digits, using formal written methods of columnar addition and subtraction | add and subtract numbers with up to 4 digits using the formal written methods of columnar addition and subtraction where appropriate | add and subtract whole numbers with more than 4 digits, including using formal written methods (columnar addition and subtraction) |  |
| **Inverse operations, estimating and checking answers** | | | | | |
|  | recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems. | estimate the answer to a calculation and use inverse operations to check answers | estimate and use inverse operations to check answers to a calculation | use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy | use estimation to check answers to calculations and determine, in the context of a problem, levels of accuracy. |
| **Problem solving** | | | | | |
| solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, and missing number problems such as 7 = 🗆 - 9 | solve problems with addition and subtraction:   * using concrete objects and pictorial representations, including those involving numbers, quantities and measures * applying their increasing knowledge of mental and written methods | solve problems, including missing number problems, using number facts, place value, and more complex addition and subtraction | solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why | solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why | solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why |
| *solve simple problems in a practical context involving addition and subtraction of money of the same unit, including giving change (copied from Measurement)* | Solve problems involving addition, subtraction, multiplication and division |

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| **Multiplication and division** | | | | | | | | | |
| **Multiplication and division facts** | | | | | | | | | |
| **Year 1** | | **Year 2** | | **Year 3** | | **Year 4** | | **Year 5** | **Year 6** |
| *count in multiples of twos, fives and tens (copied from Number and Place Value)* | *count in steps of 2, 3, and 5 from 0, and in tens from any number, forward or backward (copied from Number and Place Value)* | | *count from 0 in multiples of 4, 8, 50 and 100 (copied from Number and Place Value)* | | *count in multiples of 6, 7, 9, 25 and 1 000 (copied from Number and Place Value)* | | *count forwards or backwards in steps of powers of 10 for any given number up to 1 000 000 (copied from Number and Place Value)* | |  |
|  | recall and use multiplication and division facts for the 2, 5 and 10 multiplication tables, including recognising odd and even numbers | | recall and use multiplication and division facts for the 3, 4 and 8 multiplication tables | | recall multiplication and division facts for multiplication tables up to 12 × 12 | |  | |  |
| **Mental calculation** | | | | | | | | | |
|  |  | | write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods *(appears also in Written Methods)* | | use place value, known and derived facts to multiply and divide mentally, including: multiplying by 0 and 1; dividing by 1; multiplying together three numbers | | multiply and divide numbers mentally drawing upon known facts | | perform mental calculations, including with mixed operations and large numbers |
|  | show that multiplication of two numbers can be done in any order (commutative) and division of one number by another cannot | |  | | recognise and use factor pairs and commutativity in mental calculations *(appears also in Properties of Numbers)* | | multiply and divide whole numbers and those involving decimals by 10, 100 and 1000 | | *associate a fraction with division and calculate decimal fraction equivalents (e.g. 0.375) for a simple fraction (e.g. 3/8) (copied from Fractions)* |
| **Written calculation** | | | | | | | | | |
|  | calculate mathematical statements for multiplication and division within the multiplication tables and write them using the multiplication (×), division (÷) and equals (=) signs | | write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods *(appears also in Mental Methods)* | | multiply two-digit and three-digit numbers by a one-digit number using formal written layout | | multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers | | multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication |
|  |  | |  | |  | | divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context | | divide numbers up to 4-digits by a two-digit whole number using the formal written method of short division where appropriate for the context divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context |
|  |  | |  | |  | |  | | *use written division methods in cases where the answer has up to two decimal places (copied from Fractions)* |
| **Properties of numbers: multiples, factors, primes, square and cube numbers** | | | | | | | | | |
|  |  | |  | | recognise and use factor pairs and commutativity in mental calculations (repeated) | | identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers. | | identify common factors, common multiples and prime numbers  *use common factors to simplify fractions; use common multiples to express fractions in the same denomination (copied from Fractions)* |
| know and use the vocabulary of prime numbers, prime factors and composite (non-prime) numbers | |
| establish whether a number up to 100 is prime and recall prime numbers up to 19 | |
|  |  | |  | |  | | recognise and use square numbers and cube numbers, and the notation for squared (2) and cubed (3) | | *calculate, estimate and compare volume of cubes and cuboids using standard units, including centimetre cubed (cm3) and cubic metres (m3), and extending to other units such as mm3 and km3 (copied from Measures)* |
| **Order of operations** | | | | | | | | | |
|  |  | |  | |  | |  | | use their knowledge of the order of operations to carry out calculations involving the four operations |
| **Inverse operations, estimating and checking answers** | | | | | | | | | |
|  |  | | *estimate the answer to a calculation and use inverse operations to check answers (copied from Addition and Subtraction)* | | *estimate and use inverse operations to check answers to a calculation (copied from Addition and Subtraction)* | |  | | use estimation to check answers to calculations and determine, in the context of a problem, levels of accuracy |
| **Problem solving** | | | | | | | | | |
| solve one-step problems involving multiplication and division, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher | solve problems involving multiplication and division, using materials, arrays, repeated addition, mental methods, and multiplication and division facts, including problems in contexts | | solve problems, including missing number problems, involving multiplication and division, including positive integer scaling problems and correspondence problems in which n objects are connected to m objects | | solve problems involving multiplying and adding, including using the distributive law to multiply two-digit numbers by one digit, integer scaling problems and harder correspondence problems such as n objects are connected to m objects | | solve problems involving multiplication and division including using their knowledge of factors and multiples, squares and cubes | | solve problems involving addition, subtraction, multiplication and division |
| solve problems involving addition, subtraction, multiplication and division and a combination of these, including understanding the meaning of the equals sign | |  |
| solve problems involving multiplication and division, including scaling by simple fractions and problems involving simple rates | | *solve problems involving similar shapes where the scale factor is known or can be found*  *(copied from Ratio and Proportion)* |

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| **Fractions, decimals and percentages** | | | | | |
| **Counting in fractional steps** | | | | | |
| **Year 1** | **Year 2** | **Year 3** | **Year 4** | **Year 5** | **Year 6** |
|  | *Pupils should count in fractions up to 10, starting from any number and using the1/2 and 2/4 equivalence on the number line (Non Statutory Guidance)* | count up and down in tenths | count up and down in hundredths |  |  |
| **Recognising fractions** | | | | | |
| recognise, find and name a half as one of two equal parts of an object, shape or quantity | recognise, find, name and write fractions 1/3, 1/4, 2/4 and 3/4 of a length, shape, set of objects or quantity | recognise, find and write fractions of a discrete set of objects: unit fractions and non-unit fractions with small denominators | recognise that hundredths arise when dividing an object by one hundred and dividing tenths by ten | recognise and use thousandths and relate them to tenths, hundredths and decimal equivalents *(appears also in Equivalence)* |  |
| recognise that tenths arise from dividing an object into 10 equal parts and in dividing one – digit numbers or quantities by 10. |
| recognise, find and name a quarter as one of four equal parts of an object, shape or quantity | recognise and use fractions as numbers: unit fractions and non-unit fractions with small denominators |
| **Comparing fractions** | | | | | |
|  |  | compare and order unit fractions, and fractions with the same denominators |  | compare and order fractions whose denominators are all multiples of the same number | compare and order fractions, including fractions >1 |
| **Comparing decimals** | | | | | |
|  |  |  | compare numbers with the same number of decimal places up to two decimal places | read, write, order and compare numbers with up to three decimal places | identify the value of each digit in numbers given to three decimal places |
| **Rounding including decimals** | | | | | |
|  |  |  | round decimals with one decimal place to the nearest whole number | round decimals with two decimal places to the nearest whole number and to one decimal place | solve problems which require answers to be rounded to specified degrees of accuracy |
| **Equivalence** | | | | | |
|  | write simple fractions e.g. 1/2 of 6 = 3 and recognise the equivalence of 2/4 and 1/2. | recognise and show, using diagrams, equivalent fractions with small denominators | recognise and show, using diagrams, families of common equivalent fractions | identify, name and write equivalent fractions of a given fraction, represented visually, including tenths and hundredths | use common factors to simplify fractions; use common multiples to express fractions in the same denomination |
|  |  |  | recognise and write decimal equivalents of any number of tenths or hundredths | read and write decimal numbers as fractions (e.g. 0.71 = 71/100) | associate a fraction with division and calculate decimal fraction equivalents (e.g. 0.375) for a simple fraction (e.g. 3/8) |
| recognise and use thousandths and relate them to tenths, hundredths and decimal equivalents |
|  |  |  | recognise and write decimal equivalents to 1/4; 1/2; 3/4 | recognise the per cent symbol (%) and understand that per cent relates to “number of parts per hundred”, and write percentages as a fraction with denominator 100 as a decimal fraction | recall and use equivalences between simple fractions, decimals and percentages, including in different contexts. |
| **Addition and subtraction of fractions** | | | | | |
|  |  | add and subtract fractions with the same denominator within one whole (e.g. 5/7 + 1/7 = 6/7) | add and subtract fractions with the same denominator | add and subtract fractions with the same denominator and multiples of the same number | add and subtract fractions with different denominators and mixed numbers, using the  concept of equivalent fractions |
| recognise mixed numbers and improper fractions and convert from one form to the other and write mathematical statements > 1 as a mixed number (e.g. 2/5 + 4/5 = 6/5 = 11/5) |
| **Multiplication and division of fractions** | | | | | |
|  |  |  |  | multiply proper fractions and mixed numbers by whole numbers, supported by materials and diagrams | multiply simple pairs of proper fractions, writing the answer in its simplest form (e.g. 1/4 × 1/2 = 1/8) |
| multiply one-digit numbers with up to two decimal places by whole numbers |
|  |  |  |  |  | divide proper fractions by whole numbers (e.g. 1/3 ÷ 2 = 1/6) |
| **Multiplication and division of decimals** | | | | | |
|  |  |  |  |  | multiply one-digit numbers with up to two decimal places by whole numbers |
|  |  |  | find the effect of dividing a one- or two-digit number by 10 and 100, identifying the value of the digits in the answer as ones, tenths and hundredths |  | multiply and divide numbers by 10, 100 and 1000 where the answers are up to three decimal places |
|  |  |  |  |  | identify the value of each digit to three decimal places and multiply and divide numbers by 10, 100 and 1000 where the answers are up to three decimal places |
|  |  |  |  |  | associate a fraction with division and calculate decimal fraction equivalents (e.g. 0.375) for a simple fraction (e.g. 3/8) |
|  |  |  |  |  | use written division methods in cases where the answer has up to two decimal places |
| **Problem solving** | | | | | |
|  |  | solve problems that involve all of the above | solve problems involving increasingly harder fractions to calculate quantities, and fractions to divide quantities, including non-unit fractions where the answer is a whole number | solve problems involving numbers up to three decimal places |  |
|  |  |  | solve simple measure and money problems involving fractions and decimals to two decimal places. | solve problems which require knowing percentage and decimal equivalents of 1/2, 1/4, 1/5, 2/5, 4/5 and those with a denominator of a multiple of 10 or 25. |  |

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| **Ratio and proportion** | | | | | |
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|  |  |  |  |  | solve problems involving the relative sizes of two quantities where missing values can be found by using integer multiplication and division facts |
|  |  |  |  |  | solve problems involving the calculation of percentages [for example 15% of 360] and the use of percentages for comparison |
|  |  |  |  |  | solve problems involving similar shapes where the scale factor is known or can be found |
|  |  |  |  |  | solve problems involving unequal sharing and grouping using knowledge of fractions and multiples. |

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| **Algebra** | | | | | | |
| **Equations** | | | | | | |
| **Year 1** | **Year 2** | **Year 3** | | **Year 4** | **Year 5** | **Year 6** |
| *solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, and missing number problems such as 7 = 🗆 - 9 (copied from Addition and Subtraction)* | *recognise and use the inverse relationship between addition and subtraction and use this to check calculations and missing number problems. (copied from Addition and Subtraction)* | *solve problems, including missing number problems, using number facts, place value, and more complex addition and subtraction. (copied from Addition and Subtraction)* | |  | *use the properties of rectangles to deduce related facts and find missing lengths and angles*  *(copied from Geometry: Properties of Shapes)* | express missing number problems algebraically |
| *solve problems, including missing number problems, involving multiplication and division, including integer scaling*  *(copied from Multiplication and Division)* | |
|  | *recall and use addition and subtraction facts to 20 fluently, and derive and use related facts up to 100 (copied from Addition and Subtraction)* |  | |  |  | find pairs of numbers that satisfy number sentences involving two unknowns |
| *represent and use number bonds and related subtraction facts within 20 (copied from Addition and Subtraction)* |  |  | |  |  | enumerate all possibilities of combinations of two variables |
| **Formulae** | | | | | | |
|  |  |  | *Perimeter can be expressed algebraically as 2(a + b) where a and b are the dimensions in the same unit. (Copied from NSG measurement)* | |  | use simple formulae |
| *recognise when it is possible to use formulae**for area and volume of shapes (copied from Measurement)* |
| **Sequences** | | | | | | |
| *sequence events in chronological order using language such as: before and after, next, first, today, yesterday, tomorrow, morning, afternoon and evening*  *(copied from Measurement)* | *compare and sequence intervals of time (copied from Measurement)* |  |  | |  | generate and describe linear number sequences |
| *order and arrange combinations of mathematical objects in patterns (copied from Geometry: position and direction)* |

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| **Measurement** | | | | | |
| **Comparing and estimating** | | | | | |
| **Year 1** | **Year 2** | **Year 3** | **Year 4** | **Year 5** | **Year 6** |
| compare, describe and solve practical problems for:   * lengths and heights [e.g. long/short, longer/shorter, tall/short, double/half] * mass/weight [e.g. heavy/light, heavier than, lighter than] * capacity and volume [e.g. full/empty, more than, less than, half, half full, quarter] * time [e.g. quicker, slower, earlier, later] | compare and order lengths, mass, volume/capacity and record the results using >, < and = |  | estimate, compare and calculate different measures, including money in pounds and pence  *(also included in Measuring)* | calculate and compare the area of squares and rectangles including using standard units, square centimetres (cm2) and square metres (m2) and estimate the area of irregular shapes (also included in measuring) | calculate, estimate and compare volume of cubes and cuboids using standard units, including centimetre cubed (cm3) and cubic metres (m3), and extending to other units such as mm3 and km3. |
| estimate volume (e.g. using 1 cm3 blocks to build cubes and cuboids) and capacity (e.g. using water) |
| sequence events in chronological order using language [e.g. before and after, next, first, today, yesterday, tomorrow, morning, afternoon and evening] | compare and sequence intervals of time | compare durations of events, for example to calculate the time taken by particular events or tasks |  |  |  |
|  |  | estimate and read time with increasing accuracy to the nearest minute; record and compare time in terms of seconds, minutes, hours and o’clock; use vocabulary such as a.m./p.m., morning, afternoon, noon and midnight *(appears also in Telling the Time)* |  |  |  |
| **Measuring and calculating** | | | | | |
| measure and begin to record the following:   * lengths and heights * mass/weight * capacity and volume * time (hours, minutes, seconds) | choose and use appropriate standard units to estimate and measure length/height in any direction (m/cm); mass (kg/g); temperature (°C); capacity (litres/ml) to the nearest appropriate unit, using rulers, scales, thermometers and measuring vessels | measure, compare, add and subtract: lengths (m/cm/mm); mass (kg/g); volume/capacity (l/ml) | estimate, compare and calculate different measures, including money in pounds and pence  *(appears also in Comparing)* | use all four operations to solve problems involving measure (e.g. length, mass, volume, money) using decimal notation including scaling. | solve problems involving the calculation and conversion of units of measure, using decimal notation up to three decimal places where appropriate  *(appears also in Converting)* |
|  |  | measure the perimeter of simple 2-D shapes | measure and calculate the perimeter of a rectilinear figure (including squares) in centimetres and metres | measure and calculate the perimeter of composite rectilinear shapes in centimetres and metres | recognise that shapes with the same areas can have different perimeters and vice versa |
| recognise and know the value of different denominations of coins and notes | recognise and use symbols for pounds (£) and pence (p); combine amounts to make a particular value | add and subtract amounts of money to give change, using both £ and p in practical contexts |  |  |  |
| find different combinations of coins that equal the same amounts of money |
| solve simple problems in a practical context involving addition and subtraction of money of the same unit, including giving change |
|  |  |  | find the area of rectilinear shapes by counting squares | calculate and compare the area of squares and rectangles including using standard units, square centimetres (cm2) and square metres (m2) and estimate the area of irregular shapes  *recognise and use square numbers and cube numbers, and the notation for squared (2) and cubed (3) (copied from Multiplication and Division)* | calculate the area of parallelograms and triangles |
| calculate, estimate and compare volume of cubes and cuboids using standard units, including cubic centimetres (cm3) and cubic metres (m3), and extending to other units [e.g. mm3 and km3]. |
| recognise when it is possible to use formulae for area and volume of shapes |
| **Telling the time** | | | | | |
| tell the time to the hour and half past the hour and draw the hands on a clock face to show these times. | tell and write the time to five minutes, including quarter past/to the hour and draw the hands on a clock face to show these times. | tell and write the time from an analogue clock, including using Roman numerals from I to XII, and 12-hour and 24-hour clocks | read, write and convert time between analogue and digital 12 and 24-hour clocks *(appears also in Converting)* |  |  |
| recognise and use language relating to dates, including days of the week, weeks, months and years | know the number of minutes in an hour and the number of hours in a day. *(appears also in Converting)* | estimate and read  time with increasing accuracy to the nearest minute; record and compare time in terms of seconds, minutes, hours and o’clock; use vocabulary such as a.m./p.m., morning, afternoon, noon and midnight *(appears also in Comparing and Estimating)* |  |  |  |
|  |  |  | solve problems involving converting from hours to minutes; minutes to seconds; years to months; weeks to days *(appears also in Converting)* | solve problems involving converting between units of time |  |
| **Converting** | | | | | |
|  | know the number of minutes in an hour and the number of hours in a day.  *(appears also in Telling the Time)* | know the number of seconds in a minute and the number of days in each month, year and leap year | convert between different units of measure (e.g. kilometre to metre; hour to minute) | convert between different units of metric measure (e.g. kilometre and metre; centimetre and metre; centimetre and millimetre; gram and kilogram; litre and millilitre) | use, read, write and convert between standard units, converting measurements of length, mass, volume and time from a smaller unit of measure to a larger unit, and vice versa, using decimal notation to up to three decimal places |
|  |  |  | read, write and convert time between analogue and digital 12 and 24-hour clocks *(appears also in Converting)* | solve problems involving converting between units of time | solve problems involving the calculation and conversion of units of measure, using decimal notation up to three decimal places where appropriate  *(appears also in Measuring and Calculating)* |
|  |  |  | solve problems involving converting from hours to minutes; minutes to seconds; years to months; weeks to days *(appears also in Telling the Time)* | understand and use equivalences between metric units and common imperial units such as inches, pounds and pints | convert between miles and kilometres |

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| **Geometry: Properties of shape** | | | | | |
| **Identifying shapes and their properties** | | | | | |
| **Year 1** | **Year 2** | **Year 3** | **Year 4** | **Year 5** | **Year 6** |
| Recognise and name common 2-D and 3-D shapes, including:   * 2-D shapes [e.g. rectangles (including squares), circles and triangles] * 3-D shapes [e.g. cuboids (including cubes), pyramids and spheres]. | identify and describe the properties of 2-D shapes, including the number of sides and line symmetry in a vertical line |  | identify lines of symmetry in 2-D shapes presented in different orientations | identify 3-D shapes, including cubes and other cuboids, from 2-D representations | recognise, describe and build simple 3-D shapes, including making nets *(appears also in Drawing and Constructing)* |
| identify and describe the properties of 3-D shapes, including the number of edges, vertices and faces | illustrate and name parts of circles, including radius, diameter and circumference and know that the diameter is twice the radius |
| identify 2-D shapes on the surface of 3-D shapes, [for example, a circle on a cylinder and a triangle on a pyramid] |
| **Drawing and constructing** | | | | | |
|  |  | draw 2-D shapes and make 3-D shapes using modelling materials; recognise 3-D shapes in different orientations and describe them | complete a simple symmetric figure with respect to a specific line of symmetry | draw given angles, and measure them in degrees (o) | draw 2-D shapes using given dimensions and angles |
| recognise, describe and build simple 3-D shapes, including making nets *(appears also in Identifying Shapes and Their Properties)* |
| **Comparing and classifying** | | | | | |
|  | compare and sort common 2-D and 3-D shapes and everyday objects |  | compare and classify geometric shapes, including quadrilaterals and triangles, based on their properties and sizes | use the properties of rectangles to deduce related facts and find missing lengths and angles | compare and classify geometric shapes based on their properties and sizes and find unknown angles in any triangles, quadrilaterals, and regular polygons |
| distinguish between regular and irregular polygons based on reasoning about equal sides and angles |
| **Angles** | | | | | |
|  |  | recognise angles as a property of shape or a description of a turn |  | know angles are measured in degrees: estimate and compare acute, obtuse and reflex angles |  |
|  |  | identify right angles, recognise that two right angles make a half-turn, three make three quarters of a turn and four a complete turn; identify whether angles are greater than or less than a right angle | identify acute and obtuse angles and compare and order angles up to two right angles by size | identify:   * angles at a point and one whole turn (total 360o) * angles at a point on a straight line and ½ a turn (total 180o)   other multiples of 90o | recognise angles where they meet at a point, are on a straight line, or are vertically opposite, and find missing angles |
|  |  | identify horizontal and vertical lines and pairs of perpendicular and parallel lines |  |  |  |

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| **Geometry: Position and direction** | | | | | |
| **Position, direction and movement** | | | | | |
| **Year 1** | **Year 2** | **Year 3** | **Year 4** | **Year 5** | **Year 6** |
| describe position, direction and movement, including half, quarter and three-quarter turns. | use mathematical vocabulary to describe position, direction and movement including movement in a straight line and distinguishing between rotation as a turn and in terms of right angles for quarter, half and three-quarter turns (clockwise and anti-clockwise) |  | describe positions on a  2-D grid as coordinates in the first quadrant | identify, describe and represent the position of a shape following a reflection or translation, using the appropriate language, and know that the shape has not changed | describe positions on the full coordinate grid (all four quadrants) |
| describe movements between positions as translations of a given unit to the left/right and up/down | draw and translate simple shapes on the coordinate plane, and reflect them in the axes. |
|  |  |  | plot specified points and draw sides to complete a given polygon |  |  |
| **Pattern** | | | | | |
|  | order and arrange combinations of mathematical objects in patterns and sequences |  |  |  |  |

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| **Statistics** | | | | | |
| **Interpreting, constructing and presenting data** | | | | | |
| **Year 1** | **Year 2** | **Year 3** | **Year 4** | **Year 5** | **Year 6** |
|  | interpret and construct simple pictograms, tally charts, block diagrams and simple tables | interpret and present data using bar charts, pictograms and tables | interpret and present discrete and continuous data using appropriate graphical methods, including bar charts and time graphs | complete, read and interpret information in tables, including timetables | interpret and construct pie charts and line graphs and use these to solve problems |
|  | ask and answer simple questions by counting the number of objects in each category and sorting the categories by quantity |  |  |  |  |
|  | ask and answer questions about totalling and comparing categorical data |  |  |  |  |
| **Solving problems** | | | | | |
|  |  | solve one-step and two-step questions [e.g. ‘How many more?’ and ‘How many fewer?’] using information presented in scaled bar charts and pictograms and tables. | solve comparison, sum and difference problems using information presented in bar charts, pictograms, tables and other graphs. | solve comparison, sum and difference problems using information presented in a line graph | calculate and interpret the mean as an average |